



C09-A-102/C09-AA-102/C09-AEI-102/C09-BM-102/  
C09-C-102/C09-CM-102/C09-CH-102/C09-CHPC-102/  
C09-CHPP-102/C09-CHOT-102/C09-CHST-102/  
C09-EC-102/C09-EE-102/C09-IT-102/C09-M-102/  
C09-MET-102/C09-MNG-102/ C09-PET-102/  
C09-TT-102/C09-RAC-**102**

**3002**

**BOARD DIPLOMA EXAMINATION, (C-09)**  
**OCT/NOV—2017**  
**FIRST YEAR (COMMON) EXAMINATION**

**ENGINEERING MATHEMATICS—I**

Time : 3 hours ]

[ Total Marks : 80

**PART—A**

3×10=30

**Instructions** : (1) Answer **all** questions.

(2) Each question carries **three** marks.

1. Express  $3 - 2x + x^2$  in the form of  $A^2 - B^2$
2. If  $p = 2a + 3b$ ,  $q = 3b + 4c$ ,  $r = 5a + 2b$ , Find  $3p + 2q - 5r$ .
3. Resolve  $\frac{4}{x^2 - x - 5}$  into partial fractions.
4. If  $A + B + C = 90^\circ$ , prove that  $\cot A + \cot B + \cot C = \cot A \cot B \cot C$ .
5. Find the Modulus of  $\frac{5 + 12i}{2 - 3i}$
6. If  $\sin A = \frac{4}{5}$ , Find  $\cos 2A$  and  $\sin 2A$

/3002

1

[ Contd...

[www.ManaResults.co.in](http://www.ManaResults.co.in)

7. Find the Equation of the Circle with  $(-5,1)$  and  $(3,-7)$  as end points of a diameter.

8. Find the angle between the straight lines  $x + 5y - 7 = 0$  and  $x - 3y - 18 = 0$ .

9. Evaluate  $\lim_{x \rightarrow 1} \frac{x^2 - 3x + 2}{x^2 - 4x + 3}$

10. Differentiate  $\frac{1 + \sin x}{1 - \sin x}$  w.r.t.x.

**PART—B**

10×5=50

**Instructions :** (1) Answer *any five* questions.

(2) Each question carries **ten** marks.

11. (a) Show that

$$\begin{vmatrix} 1 & 1 & 1 \\ 1 & 1 & a \\ 1 & 1 & 1 \end{vmatrix} = b$$

(b) Find the inverse of the matrix

$$\begin{vmatrix} 1 & 1 & 1 \\ 4 & 1 & 0 \\ 8 & 1 & 1 \end{vmatrix}$$

12. (a) Solve  $\tan^2 \theta - 1 = \sqrt{3} \tan \theta - \sqrt{3} = 0$

(b) Solve the  $\triangle ABC$  if  $a = 2, c = \sqrt{3}, B = 60^\circ$ .

13. (a) If  $A+B+C=180^\circ$  prove that  $\sin 2A + \sin 2B + \sin 2C = 4 \sin A \sin B \sin C$ .

(b) Show that  $\tan^{-1} \frac{3}{4} + \tan^{-1} \frac{5}{12} = \tan^{-1} \frac{56}{33}$

14. (a) Find the <sup>\*</sup> equation of parabola whose focus is (-1,1) and directrix  $x+y+1=0$
- (b) Find the centre, vertices, eccentricity, foci, equations of directrices and lengths of latusrectum of the ellipses represented by the equation  $16x^2 + 9y^2 = 144$
15. (a) Find the centre, length of the Transverse axis, equations of the axes, of the hyperbola represented by the equation  $4x^2 - 25y^2 = 100$ .
- (b) Find the mid point of the line joining the points (7,2,9) and (9,-6,-3).
16. (a) Differentiate  $\tan^{-1} \frac{3x - x^3}{1 - 3x^2}$  with respect to  $\sin^{-1} \frac{2x}{1 - x^2}$
- (b) If  $u = \sin^{-1} \frac{x^2 - y^2}{1 - 3x^2}$ , Show that  $x \frac{u}{x} - y \frac{u}{y} = \tan u$
17. (a) Find the Equations of Tangent and normal to the curve  $y = x^2 - 2x - 3$  at the point (0,-3).
- (b) A ladder of 5m long is placed against a vertical wall. Foot of the ladder is slipping away from the wall at rate of 5cm/sec. Find the rate of descending of its top if the foot of the ladder is 3m away from the wall.
- <sup>\*</sup> 18. (a) Find the maximum and minimum values of the function  $y = \sin x$  in the interval  $0.2$  .
- (b) Time of oscillation of a simple pendulum of variable length 'l' is given by  $T = 2\sqrt{\frac{l}{g}}$  .

If the length is increased by 1%, find approximate percentage increase in its time of oscillation where 'g' is constant.

\*\*\*