Subject Code: R13102/R13

Set No - 1

### I B. Tech I Semester Regular Examinations Feb./Mar. - 2014

MATHEMATICS-I

(Common to All Branches)

**Time: 3 hours** 

Max. Marks: 70

Question Paper Consists of Part-A and Part-B Answering the question in **Part-A** is Compulsory, Three Questions should be answered from Part-B \*\*\*\*

#### **PART-A**

- Find the orthogonal trajectories of the curve  $r = a(1 + \cos \theta)$ . 1.(i)
- (ii) If  $x = rsin\theta cos\varphi$ ,  $y = rsin\theta sin\varphi$ ,  $z = r cos\theta$ , find  $\frac{\partial(r,\theta,\varphi)}{\partial(x,y,z)}$ , given that  $\frac{\partial(x,y,z)}{\partial(r,\theta,\varphi)} = r^2 sin\theta$ . (iii) Find the Laplace transform of  $f(t) = \begin{cases} t, \ 0 < t < 1 \\ 0, \ t > 1 \end{cases}$  using Heaviside function. (iv) Let the heat conduction in a thin metallic bar of length L is governed by the equation
- $\frac{\partial u}{\partial t} = a^2 \frac{\partial^2 u}{\partial x^2}$ , t > 0. If both ends of the bar are held at constant temperature zero and the bar is initially has temperature f(x), find the temperature u(x,t).
- (v) Solve  $p^2 + pq = z^2$ . (vi) Find  $\frac{1}{D^2 - 4D + 4} x^2 sinx$ . [4+4+4+3+3]

#### PART-B

- $y(2x^{2} xy + 1)dx + (x y)dy = 0$ 2.(a) Solve
  - (b) Find the complete solution of  $y'' + 2y = x^2 e^{3x} + e^x \cos 2x$ [8+8]

3.(a) Solve 
$$\frac{dy}{dx} + xsin2y = x^3 cos^2 y$$
  
(b) Find the solution of  $\frac{d^2y}{dx} + 4y = Sin 2x + cos 2x$ 

(b) Find the solution of 
$$\frac{d^2y}{dx^2} + 4y = \sin 3x + \cos 2x$$
. [8+8]

4.(a) Find the Laplace transform of 
$$f(t) = \frac{\cos at - \cos bt}{t}$$
.  
(b) If  $x = \sqrt{vw}, y = \sqrt{uw}, z = \sqrt{uv}$  and  
 $u = rsin \theta cos \varphi, v = r sin \theta sin \varphi$  and  $w = rcos \theta$ , find  $\frac{\partial(x, y, z)}{\partial(r, \theta, \varphi)}$ . [8+8]

- Expand  $f(x, y) = e^{y} \ln(1 + x)$  in powers of x and y using MacLaurin's Series 5.(a)
  - Solve  $y'' 8y' + 15y = 9te^{2t}$ , y(0) = 5 and y'(0) = 10 using Laplace transforms (b)

$$[8+8]$$

- 6.(a) Solve  $(y + xz)p (x + yz)q = x^2 y^2$ . (b) Solve the partial differential equation px+qy = 1. [8+8]
- 7.(a) Find the partial differential equation of all spheres whose centers lie on z- axis.
  - Find the solution of the wave equation  $\frac{\partial^2 u}{\partial t^2} = a^2 \frac{\partial^2 u}{\partial x^2}$ , if the initial deflection is (b)

$$f(x) = \begin{cases} \frac{2k}{l}x & \text{if } 0 < x < l/2\\ \frac{2k}{l}(l-x) & \text{if } \frac{l}{2} < x < l \end{cases} \text{ and initial velocity equal to } 0.$$

$$[8+8]$$

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Subject Code: R13102/R13

Set No - 2

I B. Tech I Semester Regular Examinations Feb./Mar. - 2014

MATHEMATICS-I

(Common to All Branches)

**Time: 3 hours** 

Max. Marks: 70

Question Paper Consists of Part-A and Part-B Answering the question in **Part-A** is Compulsory, Three Questions should be answered from Part-B \*\*\*\*

#### **PART-A**

Find the complete solution of  $(D^4 + 16)y = 0$ . 1.(i)

(ii) If 
$$x = r\cos\theta$$
,  $y = r\sin\theta$ ,  $z = z$ , find  $\frac{\partial(r,\theta,z)}{\partial(x,y,z)}$ , given that  $\frac{\partial(x,y,z)}{\partial(r,\theta,z)} = r$ .

- (iii) Solve  $x^2p^2 + y^2q^2 = z^2$ .
- (iv) Find the solution, by Laplace transform method, of the integro-differential equation  $y' + 3y + 2\int_0^t y(t)dt = t$
- Find the differential equation of the orthogonal trajectories for the family of parabola (v) through the origin and foci on y-axis.
- (vi) Find the solution of wave equation in one dimension using the method of separation of variables.

[3+3+4+4+4+4]

[8+8]

[8+8]

[8+8]

- $\frac{\mathbf{PART-B}}{y(y^2-2x^2)dx+x(2y^2-x^2)dy=0}$ Solve 2.(a)
  - Find the complete solution of y'' + 5y' 6y = sin4x sinx. (b)

3.(a) Solve 
$$\cos x \, dy = y(\sin x - y)dx$$
.  
(b) Find the solution of  $\frac{d^2y}{dx^2} - 4\frac{dy}{dx} + 3y = 2xe^{3x} + 3e^x \cos 2x$ .

- Find the Laplace transform of  $f(t) = \int_0^t e^{-u} \cos u \, du$ . 4.(a) Find the shortest distance from origin to the surface  $xyz^2 = 2$ . (b)
- Find  $\frac{\partial(u,v)}{\partial(r,\theta)}$  if u = 2axy and  $v = a(x^2 y^2)$ , where  $x = r\cos\theta$  and  $y = r\sin\theta$ . Solve  $y'' 8y' + 15 y = 9te^{2t}$ , y(0) = 5 and y'(0) = 10 using Laplace transforms 5.(a)
  - (b) [8+8]
- 6.(a) Form the partial differential equation by eliminating the arbitrary function from xyz = f(x + y + z).

(b) Find the solution of 
$$(D^2 - DD' - 2D'^2)z = (y - 1)e^x$$
, where  $D = \frac{\partial}{\partial x}$  and  $D' = \frac{\partial}{\partial y}$ .  
[8+8]

- 7.(a) Solve the partial differential equation xzp + yzq = xy.
  - (b) Find the temperature in a bar of length l which is perfectly insulated laterally and whose ends O and A are kept at 0°C, given that the initial temperature at any point P of the rod is given by f(x).

[8+8]

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Set No - 3

## I B. Tech I Semester Regular Examinations Feb./Mar. - 2014

MATHEMATICS-I

(Common to All Branches)

**Time: 3 hours** 

Subject Code: R13102/R13

Max. Marks: 70

Question Paper Consists of Part-A and Part-B Answering the question in **Part-A** is Compulsory, Three Questions should be answered from Part-B \*\*\*\*

#### **PART-A**

- Find the dimensions of rectangular box of maximum capacity whose surface area is S. 1.(i)
- Find the orthogonal trajectories of the family of curves  $x^{2/3} + y^{2/3} = a^{2/3}$ . (ii)
- (iii) A generator having emf 100 volts is connected in series with a 10 ohm resistor and an inductor of 2 henries. If the switch is closed at a time t = 0, find the current at time t > 0.
- (iv) Find the Laplace transform of  $f(t) = \begin{cases} t, & 0 < t < 1 \\ 0, & t > 1 \end{cases}$  using Heaviside function.
- (v) Solve pq+qx = y.
- (vi) Find the solution of  $2x \frac{\partial z}{\partial x} 3y \frac{\partial z}{\partial y} = 0$  by the method of separation of variables.

[4+4+4+3+3]

[8+8]

[8+8]

[8+8]

- $\frac{\mathbf{PART-B}}{y(1+xy)dx + x(1-xy)dy = 0}$ Solve 2.(a)
- Find the complete solution of  $y'' + 4y = e^x sin^2 x$ . (b)

3.(a) Solve 
$$2x y' + y = \frac{2x^2}{y^3}, y(1) = 2.$$

Find the solution of  $\frac{d^2y}{dx^2} - 4\frac{dy}{dx} - 5y = e^{2x} + 3\cos(4x+3).$ (b)

- Find the Laplace transform of  $f(t) = te^{-2t}\cos t$ . Find the maxima and minima of  $x^3 + 3xy^2 15x^2 15y^2 + 72x$ . 4.(a) (b)
- 5.(a)
- Expand  $f(x, y) = e^{xy}$  in powers of (x-1) and (y-1). Solve  $y'' + 7y' + 10 y = 4e^{-3t}$ , y(0) = 0 and y'(0) = -1 using Laplace transforms. (b) [8+8]
- Form the partial differential equation by eliminating the arbitrary constants 'a' and 'b' 6.(a) from  $2z = \frac{x^2}{a^2} + \frac{y^2}{b^2}$ .

(b) Find the solution of 
$$(4D^2 + 12DD' + 9{D'}^2)z = e^{3x-2y}$$
, where  $D = \frac{\partial}{\partial x}$  and  $D' = \frac{\partial}{\partial y}$ .  
[8+8]

- 7.(a) Solve the partial differential equation  $p \tan x + q \tan y = \tan z$ .
- (b) A tightly stretched string with fixed end points x=0 and x=1 is initially in a position given by  $y = y_0 sin^3 \frac{\pi x}{l}$ . If it is released from rest from this position, find the displacement v(x,t).

[8+8]

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### I B. Tech I Semester Regular Examinations Feb./Mar. - 2014

MATHEMATICS-I

(Common to All Branches)

**Time: 3 hours** 

Subject Code: R13102/R13

Max. Marks: 70

Set No - 4

Question Paper Consists of **Part-A** and **Part-B** Answering the question in **Part-A** is Compulsory, Three Questions should be answered from **Part-B** \*\*\*\*\*

#### PART-A

- 1.(i) Find the distance from the centre at which the velocity in simple harmonic motion will be 1/3rd of the maximum.
  - (ii) Find a point with in a triangle such that the sum of the squares of its distances from the three vertices is minimum.
  - (iii) Find the solution, by Laplace transform method, of the integro-differential equation  $y' + 4y = \int_0^t y(t)dt$ , y(0) = 0.
  - (iv) Uranium disintegrates at a rate proportional to the amount present at that time. If M and N grams of Uranium that rae present at times  $T_1$  and  $T_2$  respectively, find the half life of Uranium.
- (v) Find the complete solution of  $(D^3 3D^2D' + 3DD'^2 D'^3)z = 0$ .

(vi) Solve 
$$z^2 = 1 + p^2 + q^2$$
.  
[4+4+4+3+3]

#### PART-B

2.(a) Solve 
$$(3y^2 + 4xy - x)dx + x(x + 2y)dy = 0$$

(b) Find the solution of 
$$\frac{d^2y}{dx^2} + 5\frac{dy}{dx} - 6y = sin4x \cos x$$
.

3.(a) Find the complete solution of  $y'' + 2y = x^2 e^{3x} + e^x \cos 2x$ .

(b) Solve 
$$x z' + z \log z = z (\log z)^2$$
.

4.(a) Find the Laplace transform of 
$$f(t) = te^{2t}cos 2t$$
.

(b) If 
$$u = \sin^{-1}(\frac{x^3 + y^3}{\sqrt{x} + \sqrt{y}})$$
, prove that  $xu_x + yu_y = \frac{5}{2}\tan u$ .

5.(a) If 
$$w = (y - z)(z - x)(x - y)$$
, find the value of  $\frac{\partial w}{\partial x} + \frac{\partial w}{\partial y} + \frac{\partial w}{\partial z}$ .

(b) Solve 
$$y'' + 2y' + 5y = e^{-t} \sin t$$
,  $y(0) = 0$  and  $y'(0) = 1$  using Laplace transforms.

[8+8]

[8+8]

[8+8]

[8+8]

[8+8]

6.(a) Form the partial differential equation by eliminating the arbitrary constants 'a' and 'b' from  $z = ax + by + a^2 + b^2$ .

(b) Using method of separation of variables, solve 
$$u_{xt} = e^{-t} cosx$$
 with  $u(x, 0) = u(0, t) = 0$ .  
[8+8]

- 7.(a) Find the temperature in a thin metal rod of length L, with both ends insulated and with initial temperature in the rod is  $sin(\frac{\pi x}{L})$ .
  - (b) Solve the partial differential equation  $p x^2 + qy^2 = z^2$ .

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