

I B. Tech I Semester Supplementary Examinations, Jul/August - 2021
MATHEMATICS-II (MM)

(Com. to ECE, EEE, EIE, Bio-Tech, E Com E, Agri E)

Time: 3 hours

Max. Marks: 70

- Note: 1. Question paper consists of two parts (**Part-A** and **Part-B**)
 2. Answering the question in **Part-A** is Compulsory
 3. Answer any **THREE** Questions from **Part-B**

PART -A

1. a) Prove that $E = e^{hD}$ where D is the differential operator. (4M)
- b) Solve $3x = 1 + \cos x$ using Iteration method. (4M)
- c) Evaluate $y(0.1)$ by Euler's method for $\frac{dy}{dx} = x + y$, $y(0) = 1$. (3M)
- d) Find the half range sine series of $f(x) = \sin 2x$ in $[0, 1]$. (4M)
- e) Find the finite Fourier sine transform of $f(x) = 1$ in $[0, 1]$ (4M)
- f) Find the z -transform of the sequence $\{-3, 2, 5, 0, 12\}$ (3M)

PART -B

2. a) Find $f(25)$ using Gauss Forward interpolation formula from the following table (8M)

x	10	20	30	40
y	11	20	44	80

- b) Find polynomial which is passing through the following points (8M)
 $(1, 2), (2, 5), (4, 12), (5, 33)$
3. a) Find the positive root of $2x - \log_{x_{10}} = 7$ using Newton Raphson Method. (8M)
- b) Find the positive root of $xe^x = 3$ using False position Method. (8M)
4. a) Find $y(0.1)$ using Runge-Kutta method of second order, given that $y' = x - y^2$, $y(0) = 1$ (8M)
- b) Find $y(0.1)$ by Taylor's series method given that $\frac{dy}{dx} = \frac{y-x}{y+x}$, $y(0) = 1$ (8M)
5. a) Find the Fourier series of $f(x) = e^x$ in $(0, 2)$. (8M)
- b) Find the Half range cosine series of $f(x) = \cos ax$ in $[0, \pi]$. (8M)

6. a) Using Fourier integral, Show that $\int_0^{\infty} \frac{\sin \pi \lambda}{1-\lambda^2} \sin \lambda x d \lambda = \begin{cases} \frac{1}{2} \pi \sin x & \text{if } 0 < x < \pi \\ 0 & \text{if } x > \pi \end{cases}$ (8M)

b) Find the Fourier transform of $e^{-\frac{x^2}{2}}$ ($-\infty < x < \infty$) (8M)

7. a) Find (i) $Z^{-1}\left[\frac{z}{z^2+7z+10}\right]$ (ii) $Z[e^{-an} \sin n\theta]$ (8M)

b) Solve the difference equation $y_{n+2} - 3y_{n+1} + 2y_n = 3^n$ $y_0 = 0, y_1 = 1$ using Z-Transforms (8M)