

MATHEMATICS-I

(Common to all branches)

Time: 3 hours**Max. Marks: 70**

Question Paper Consists of **Part-A** and **Part-B**
 Answering the question in **Part-A** is Compulsory,
Four Questions should be answered from **Part-B**

PART-A

1. (a) Find the orthogonal trajectory of $r = \frac{2a}{1 + \cos \theta}$
- (b) Find the P.I of $(D + 2)^2 y = x^2$
- (c) Find $L(f(t))$ where $f(t) = \begin{cases} e^t & \text{if } 0 < t < 1 \\ 0 & \text{if } t > 1 \end{cases}$
- (d) Evaluate $L^{-1} \left[\frac{2s^2 - 1}{(s^2 + 1)(s^2 + 4)} \right]$
- (e) Find $\frac{du}{dx}$ If $u = \sin(x^2 + y^2)$, where $a^2 x^2 + b^2 y^2 = c^2$
- (f) Solve the PDE $pq + (px + qy - z)^3 = 1$
- (g) Classify the Nature of PDE $\frac{\partial^2 u}{\partial x^2} + 2 \frac{\partial^2 u}{\partial x \partial y} + 4 \frac{\partial^2 u}{\partial y^2} = 0$

[7 x 2 = 14]

PART-B

2. (a) Solve the D.E $\frac{dy}{dx} = \frac{x^2 + y^2 + 1}{2xy}$
 - (b) A resistance of 100 ohms, an inductance of 0.5 Henry is connected in series with a battery of 20 volts. Find the current in the circuit, if initially there is no current in the circuit
- [7+7]
3. (a) Solve the D.E $(D^3 + 1)y = \cos(2x - 1) + x^2 e^{-x}$
 - (b) Consider an electrical circuit containing an inductance L, Resistance R and capacitance C. let q be the electrical charge on the condenser plate and 'i' be the current in the circuit at any time. Given that L = 0.25 henries, R = 250 ohms, q = 2×10^{-6} farads and there is no applied E.M.F in the circuit. At time zero the current is zero and the charge is 0.002 coulomb. Then find the charge (q) and current (i) at any time.

[7+7]



4. (a) Evaluate $L^{-1} \left[\frac{1}{2} \log \left\{ \frac{s^2 + b^2}{s^2 + a^2} \right\} \right]$

(b) Solve $(D^2 - 1)x = a \cosh t$ if $x(0) = 0, x'(0) = 0$. using Laplace transform method.

[7+7]

5. (a) Find the dimensions of a rectangular parallelepiped box open at the top of max capacity whose surface area is 108 sq inches.

(b) If $u = x + y + z, u^2v = y + z, u^3w = z$ then find $J \left(\frac{u, v, w}{x, y, z} \right)$

[7+7]

6. (a) Solve $x(y^2 + z)p - y(x^2 + z)q = z(x^2 - y^2)$

(b) Solve the PDE $p^2q^2 + x^2y^2 = x^2q^2(x^2 + y^2)$

[7+7]

7. (a) Solve the PDE $(D + D^1 - 1)(D + 2D^1 - 3)z = 4 + 3x + 6y$

(b) Solve the PDE $\frac{\partial^2 z}{\partial x^2} + 2 \frac{\partial^2 z}{\partial x \partial y} + \frac{\partial^2 z}{\partial y^2} = 2 \sin y - x \cos y$

[7+7]



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PART-A

1. (a) Solve the D.E $(x + 2y^3) \frac{dy}{dx} = y$
 (b) Find the P.I of $(D-1)^2 (D+2)y = e^x$
 (c) Find $L(\sin 2t \sin 3t)$
 (d) Evaluate $L^{-1} \left[\frac{3s+1}{(s+1)^4} \right]$
 (e) Find $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y}$ if $u = f(x+y, x-y)$
 (f) Solve the PDE $pq = p + q$.
 (g) Solve the PDE $\frac{\partial^2 z}{\partial x^2} - \frac{\partial^2 z}{\partial x \partial y} + \frac{\partial z}{\partial y} - z = 0$

[7 x 2 = 14]

PART-B

2. (a) Find the Orthogonal trajectory of the family of confocal conics $\frac{x^2}{a^2} + \frac{y^2}{a^2 + \lambda} = 1$, where λ is a Parameter.
 (b) The number of N of bacteria in a culture grew at a rate proportional to N. The value of N was initially 100 and increased to 332 in one hour. What was the value of N after 3/2 hours?
 [7+7]
3. (a) Solve the D.E $(D^2 + 1)y = \sec^2 x$ by the Method of variation parameters
 (b) Consider an electrical circuit containing an inductance L, Resistance R and capacitance C. Let q be the electrical charge on the condenser plate and 'i' be the current in the circuit at any time. There is applied E.M.F $E \sin \omega t$ in the circuit. Then find the charge on the capacitor.
 [7+7]
4. (a) Evaluate $\int_0^{\infty} e^{-t} \frac{\sin^2 t}{t} dt$ using Laplace transform
 (b) Solve $(D^4 - k^4)y = 0$ if $y(0) = 1, y^1(0) = 0, y^{11}(0) = 0, y^{111}(0) = 0$. using Laplace transform method
 [7+7]



5. (a) Find the point in the plane $2x + 3y - z = 5$ which is nearest to the origin.
(b) Prove that $u = x\sqrt{1 - y^2} + y\sqrt{1 - x^2}$, $v = \sin^{-1}(x) + \sin^{-1}(y)$ are functionally dependent and find the relation between them. [7+7]
6. (a) Solve the PDE $z(y - x) = qy^2 - px^2$
(b) Solve the PDE $z^2(p^2 + q^2) = x^2 + y^2$ [7+7]
7. (a) Solve the PDE $(D^2 - DD^1 - 2D)z = \sin(4y + 3x)$
(b) Solve $\frac{\partial^2 z}{\partial x^2} - 6\frac{\partial^2 z}{\partial x \partial y} + 9\frac{\partial^2 z}{\partial y^2} = 12x^2 + 36xy$ [7+7]



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PART-A

1. (a) Write the working Rule to find the orthogonal trajectory of the curve $f(x, y, c) = 0$
- (b) Solve the D.E $(D^2 + 1)^2 (D - 1)y = 0$
- (c) Find $L(\sqrt{t}e^{-3t})$
- (d) Evaluate $L^{-1}\left[\frac{1}{s(s+1)^3}\right]$
- (e) Find $x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y}$ if $u = \sin^{-1}\left[\frac{x^2y^2}{x+y}\right]$
- (f) Form the partial differential equation by eliminating a and b from $z = (x^2+a)(y^2+b)$
- (g) Find the P.I of $(D - D^1 - 1)(D - D^1 - 2)z = e^{2x-y}$

[7 x 2 = 14]

PART-B

2. (a) Solve the D.E : $(x^3y^2 + x)dy + (x^2y^3 - y)dx = 0$
 - (b) If the temp of a cup of coffee is 92°C when freshly poured in a room having temperature 24°C , in one minute it was cooled to 80°C . How long a period must elapse, before the temp. of the cup becomes 65°C ? A body kept in air with temp 25°C cools from 140°C to 80°C in 20 minutes. Find when the body cools down to 35°C .
3. (a) Solve the D.E $(D^2 + 3D + 2)y = xe^x \sin x$
 - (b) Consider an electrical circuit containing an inductance L, Resistance R and capacitance C. let q be the electrical charge on the condenser plate and 'i' be the current in the circuit at any time. Given that L = 0.1 henries, R = 20 ohms, $q = 25 \times 10^{-6}$ farads and there is no applied E.M.F in the circuit. At time zero the current is zero and the charge is 0.05 coulomb. Then find the charge (q) and current (i) at any time

[7+7]

[7+7]



4. (a) Find Laplace transform of unit impulse function
(b) Solve $(D^3 + D^2)x = 6t^2 + 4$ if $x(0) = 0, x'(0) = 2, x''(0) = 0$. using Laplace transform method. [7+7]
5. (a) Find the Maximum and minimum distance of the point (1, 2, 3) from the sphere $x^2 + y^2 + z^2 = 1$
(b) Expand $xy^2 + \cos xy$ in powers of $(x-1)$ and $(y-\pi/2)$ up to second degree terms. [7+7]
6. (a) Solve the PDE $x^2 p^2 + y^2 q^2 = 1$
(b) Solve the PDE $(y + z)p - (z + x)q = x - y$ [7+7]
7. (a) Solve the PDE $\frac{\partial^2 z}{\partial x^2} + \frac{\partial z}{\partial x \partial y} - 6 \frac{\partial^2 z}{\partial y^2} = y \cos x$
(b) Solve the PDE $(D^3 - 7DD'^2 - 6D'^3)Z = \sin(x + 2y) + e^{2x+y}$ [7+7]



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PART-A

1. (a) Solve the D.E $(1 + y \cos)dx + \sin x dy = 0$
- (b) A particle is executing simple harmonic motion with amplitude 5 meters and time 4 seconds. Find the time required by the particle in passing between points which are at distances 4 and 2 meters from the centre of the force and is on the same side of it.
- (c) Find $L(f(t))$ where $f(t) = \begin{cases} \cos\left(t - \frac{2\pi}{3}\right) & \text{if } t > \frac{2\pi}{3} \\ 0 & \text{if } t < \frac{2\pi}{3} \end{cases}$
- (d) Evaluate $L^{-1}\left\{\frac{1}{(s^2 + 1)(s^2 + 9)}\right\}$
- (e) If $u = \sqrt{x^2 + y^2}$, $v = \tan^{-1}\left(\frac{y}{x}\right)$ then find $J\left(\frac{u, v}{x, y}\right)$
- (f) From the partial differential equation of from by eliminating f and g from $z = f(y) + g(x + y)$.
- (g) Find the P.I of $(D^2 + 3DD^1 + 2D^1^2)z = 12xy$

[7 x 2 = 14]

PART-B

2. (a) Show that the family of curves $r^n = a \sec n\theta$ & $r^n = b \operatorname{cosec} n\theta$ are orthogonal
 - (b) A voltage Ee^{-at} is applied to a circuit containing Inductance L and resistance R, then find the current in the circuit, if initially there is no current in the circuit
- [7+7]
3. (a) Solve the D.E $(D^4 + 2D^2 + 1)y = x^2 \cos x$
 - (b) Consider an electrical circuit containing an inductance L, Resistance R and capacitance C. Let q be the electrical charge on the condenser plate and 'i' be the current in the circuit at any time. Given that L = 0.1 henries, R = 2 ohms, q = 1/260 farads and there is applied E.M.F 100sin 60t in the circuit. At time zero the current and the charge are both zero. Then find the charge on the capacitor and current in the circuit.

[7+7]



4. (a) State convolution theorem and use it to evaluate $L^{-1} \left[\frac{1}{(s^2 + 4s + 13)^2} \right]$
(b) Solve $(D^3 + D)x = 2$ if $x(0) = 3, x'(0) = 1, x''(0) = -2$. using Laplace transform method [7+7]
5. (a) Find the extreme points of $f(x, y) = 1 - x^2 - y^2$
(b) Expand $Tan^{-1} \left(\frac{y}{x} \right)$ in powers of $(x-1)$ and $(y-1)$ up to third degree terms hence evaluate $f(1.1, 0.9)$ approximately. [7+7]
6. (a) Solve the PDE $p \cos(x+y) + q \sin(x+y) = z$
(b) Solve the PDE $(x+y)(p+q)^2 + (x-y)(p-q)^2 = 1$ [7+7]
7. (a) Solve $(D^2 - D'^2 - 3D + 3D')z = xy + e^{x+2y}$
(b) Solve the PDE $\frac{\partial^2 z}{\partial x^2} - \frac{\partial z}{\partial x \partial y} - 2 \frac{\partial^2 z}{\partial y^2} = (y-1)e^x$ [7+7]

