

**I B. Tech I Semester Supplementary Examinations, May - 2018**  
**MATHEMATICS-II (NM&CV)**  
 (Com to ECE, EIE, ECom E)

Time: 3 hours

Max. Marks: 70

- Note: 1. Question Paper consists of two parts (**Part-A** and **Part-B**)  
 2. Answer **ALL** the questions in **Part-A**  
 3. Answer any **FOUR** Questions from **Part-B**

**PART -A**

1. a) Find the  $\sqrt{15}$  using Bisection method. (2M)  
 b) Construct the difference table for the following data. (2M)
- |   |   |    |    |    |
|---|---|----|----|----|
| x | 0 | 5  | 10 | 15 |
| y | 2 | 10 | 23 | 29 |
- c) Evaluate  $\int_0^1 x^2 dx$  using Trapezoidal Rule (taking n = 5). (2M)  
 d) Show that the function  $f(z)=z$  is continuous. (2M)  
 e) If C is a simple closed curve then evaluate  $\int_C (\sin 3z + z^4 + e^z) dz$  (2M)  
 f) Determine the poles of  $f(z) = \frac{z^2}{z^4+1}$  (2M)  
 g) Find the singularity of  $f(z) = \frac{\sin(z-2)}{z-2}$  at  $z = 2$ . (2M)

**PART -B**

2. a) Find the root of the equation  $x^3 - x - 4 = 0$  using False position method. (7M)  
 b) Find the root of the equation  $e^x \sin x = 1$  using Newton Raphson method. (7M)
3. a) Given that  $\sin 45^\circ = 0.7077$ ,  $\sin 50^\circ = 0.766$ ,  $\sin 55^\circ = 0.8192$ ,  $\sin 60^\circ = 0.866$  find  $\sin 48^\circ$  using Newton's forward difference formula. (7M)  
 b) Using Gauss Forward difference formula find  $y(8)$  from the following table. (7M)

X	0	5	10	15	20	25
Y	7	11	14	18	24	32

4. a) Evaluate  $\int_0^{\frac{1}{2}} \frac{dx}{\sqrt{1-x^2}}$  by (i) Simpson's 1/3<sup>rd</sup> rule (iii) Simpson's 3/8<sup>th</sup> Rule. (7M)  
 b) Solve  $\frac{dy}{dx} = xy$  using Modified Euler's method for  $x=1.1$  given  $y(1)=1$  (7M)

5. a) Prove that  $f'(z)$  does not exist at  $z=0$  if (7M)

$$f(z) = \begin{cases} \frac{x^3 y(y-ix)}{x^6 + y^2} & \text{if } z \neq 0 \\ 0 & \text{if } z = 0 \end{cases}$$

- b) Determine analytic function whose real part is  $u = \frac{\sin 2x}{\cosh 2y - \cos 2x}$  (7M)

6. a) Evaluate  $\int_C \frac{e^z}{(z^2 + \pi^2)^2} dz$  where  $C: |z| = 4$  using Cauchy's integral formula. (7M)

- b) Expand  $f(z) = \frac{1}{z(z^2 - 3z + 2)}$  in  $0 < |z| < 1$  using Laurent's expansion. (7M)

7. a) Evaluate  $\oint_C \frac{\tan z}{z^2 - 1} dz$  Where  $C: |z| = 1.5$  by Cauchy's Residue theorem. (7M)

- b) Evaluate  $\int_0^{2\pi} \frac{\cos n\theta}{1 + a^2 + 2a \cos \theta} d\theta$  where  $n$  is a positive integer,  $0 < a < 1$  (7M)