

I B. Tech II Semester Supplementary Examinations, January/February - 2023
MATHEMATICS-II (Mathematical Methods)

(Common to AE, AME, Bio-Tech, Chem E, CE, EEE, ME, Metal E, Min E, PCE, PE)

Time: 3 hours

Max. Marks: 70

- Note: 1. Question Paper consists of two parts (Part-A and Part-B)*
2. Answer ALL the question in Part-A
3. Answer any FOUR Questions from Part-B

PART -A (14 Marks)

1. a) Find the interval of existence of equation $\log_e x = \cos x$. [2M]
- b) Find the half range sine series of $f(x) = 1$ in $[0, \pi]$. [2M]
- c) Find the finite Fourier sine transform $f(x) = 1$ in $[0, 2]$. [2M]
- d) Find $\Delta(\tan^{-1}x)$ if $h = 1$. [2M]
- e) Find $y(0.1)$ given that by Euler's method $\frac{dy}{dx} = x + 2y$, $y(0) = 1$. [2M]
- f) Write the merits of modified Euler's theorem. [2M]
- g) Write one dimensional Wave equation. [2M]

PART -B (56 Marks)

2. a) Find the Real root of $x \tan x + 1 = 0$ using False position method. [7M]
- b) Evaluate $x^3 + 2x^2 + 0.4 = 0$ using Newton Raphson method. [7M]
3. a) Find $f(21)$ if $f(17) = 5.474$, $f(18) = 6.050$, $f(19) = 6.686$, $f(20) = 7.389$ using Newton Backward interpolation formula. [7M]
- b) Evaluate $y(x)$ from the following table. [7M]

x	0	1	3	4
y	2	3	4	5

4. a) Evaluate $\int_0^\pi x \sin x dx$ using Trapezoidal Rule. [7M]
- b) Using Picard's method find $y(0.1)$, $y(0.2)$ given that $\frac{dy}{dx} = x - y$, $y(0) = 2$. [7M]
5. a) Find the Fourier series of $f(x) = |x|$ in $(-\pi, \pi)$ [7M]
- b) Find the Half range cosine series of $f(x) = \cos\left(\frac{\pi x}{l}\right)$, $0 < x < l$ [7M]
6. a) Solve $\frac{\partial^2 u}{\partial x \partial t} = e^{-t} \cos x$ given that $u(x, 0) = 0$, $\frac{\partial u}{\partial t}(0, t) = 0$ [7M]
- b) Find the temperature in a bar of length 1 which is perfectly insulated laterally and whose ends O and A are kept at 0° C given that the initial temperature at any point P of the rod is given by $f(x)$. [7M]
7. a) Find the Fourier Cosine transform of $f(x)$ defined by $f(x) = \frac{1}{x}$ [7M]
- b) Find the Fourier transform of $f(x)$ defined by $f(x) = \begin{cases} x^2 & \text{if } |x| < 1 \\ 0 & \text{if } |x| > 1 \end{cases}$ [7M]
