# II B. Tech I Semester Supplementary Examinations, Oct/Nov - 2016 MATHEMATICS - III 

(Com. to CE, CHEM, BT, PE)
Time: 3 hours
Max. Marks: 75
Answer any FIVE Questions
All Questions carry Equal Marks

1. a) State and prove orthogonal property of Bessel's function
b) Express $x-\frac{5}{3} x^{3}$ as Legendre's polynomial
2. a) Find ' $k$ ' such that $f(x, y)=x^{3}+3 k x y^{2}$ is harmonic and find its harmonic conjugate
b) Prove that $\mathrm{f}(\mathrm{z})=\operatorname{sinz}$ is analytic everywhere in the complex plane and also find $f^{1}(z)$
3. a) Find all the roots of $\cos z=1 / 2$
b) Find real and imaginary parts of tanz
4. a) Evaluate $\int_{(1,1)}^{(2,4)} z^{2} d z$ along the parabola $\mathrm{x}=\mathrm{t}, \mathrm{y}=\mathrm{t}^{2}$
b) Evaluate $\int_{c} \frac{z^{2}-1}{\left(z^{2}+1\right)} d z$ along $c:|z-i|=1$
5. a) Expand $f(z)=\frac{z}{z^{2}+1}$ about $|z-3 i|>2$ by Laurent's series
b) Find the zeros and poles of (i) $f(z)=e^{\tan z}$ (ii) $\mathrm{f}(\mathrm{z})=(\mathrm{z}-1)^{3}$
6. a) Evaluate $\int_{c} \frac{2 z-1}{z(z+2)(2 z+1)} d z$ around $c:|z|=2$ by Residue theorem
b) Evaluate $\int_{0}^{2 \pi} \frac{d \theta}{(a+b \cos \theta)}$ by Residue theorem
7. a) State and prove Maximum Modulus principle.
b) Use Rouche's theorem, find the number of zero's of $z^{10}-6 z^{7}+3 z^{3}+1$
8. a) Discuss the transformation $w=\operatorname{coshz}$
b) Find the image of the strip $0<y<1 / 2$ under the transformation $w=1 / z$
