## 4424

# BOARD DIPLOMA EXAMI NATI ON, (C-14) <br> MARCH / APRI L-2019 <br> DCME - FOURTH SEMESTER EXAMI NATI ON ENGINEERING MATHEMATICS-III 

Time: 3 Hours
Max.Marks: 80

## PART-A

$$
10 \times 3=30 \mathrm{M}
$$

Instruction : 1) Answer all questions. Each question carries three marks.
2) Answers should be brief and stright to the point and shall not exceed five simple sentences.

1) Solve $\left(D^{2}+6 D+4\right) y=0$
2) Solve $\left(D^{3}-5 D^{2}+8 D-4\right) y=0$
3) Find the particular integral for $\left(D^{2}+9\right) y=e^{3 x}$
4) State the first shifting and second shifting theorems of Laplace transforms.
5) Find $L\left\{\sin ^{2} t\right\}$
6) Find L\{te $\left.{ }^{-t}\right\}$
7) Find the inverse laplace transform of $\frac{6}{s^{2}+4}+\frac{1}{s-6}+\frac{1}{s^{2}}$.
8) Write the formulae for fouries seris of a function $f(x)$ in the interval [ $c, c+2 l]$.
9) If $f(x)=x$ in $(-\pi, \pi)$ what is the values of " $a_{1}$ " in fourier series of $f(x)$.
10) Two dice are thrown. Find the probability that none of the dice shows number 2 given that their sum is 7 .

WWW.MANARESULTS.CO.IN

## PART-B

$10 \times 5=50 \mathrm{M}$
Instructions:1) Answer any Five questions.
2) Each question carriesTen marks.
3) Answers should be comprehensive and criteria for valuation is the content but not the length of the answer.
11) (a) Solve $\left(D^{2}+2 D-8\right) y=e^{-3 x}+e^{-4 x}$
(b) Solve $\left(D^{2}+2 D+4\right) y=\sin 2 x$
12) (a) solve $\left(D^{2}-1\right) y=1+\cos 2 x$.
(b) Find the particular integral of $\left(D^{2}+1\right) y=x$
13) (a) Find $L\left\{t e^{-2 t} \sin 3 t\right\}$
(b) Find $\mathrm{L}\left\{\frac{e^{t}+\cos t}{t}\right\}$
14) (a) Find $\mathrm{L}^{-1}\left\{\frac{s+2}{s^{2}+4 s+8}\right\}$
(b) Using convolution theorem find $\mathrm{L}^{-1}\left\{\frac{1}{(x-a)(x-b)}\right\}$
15) Obtain the fourier series for the functilon $f(x)=x^{2}$ for the interval $(-\pi, \pi)$.
16) Obtain the fourier sine series for the function $f(x)=e^{x}$ for the interval $(0, \pi)$
17) Find $\mathrm{p}(A \cup B)$ if
(a) $\mathrm{p}(\mathrm{A})=\frac{1}{2}, P(B)=\frac{1}{4}, P(A \cap B)=\frac{1}{8}$
(b) $\mathrm{p}(\mathrm{A}) 0.25, \mathrm{P}(\mathrm{B})=0.5, P(A \cap B)=0.16$
(c) $\mathrm{p}(\mathrm{a}) \frac{2}{7}, P(B)=\frac{3}{5} ; \mathrm{A}$ and B are disjoint
18) (a) A book containing 100 pages is opened at random. Find the probability that on the page a doublet is found
(b) If a page is randomly selected from a book of 100 pages, then find the probability that the sum of the digits of the pages is 10 .

