## 4424

## BOARD DIPLOMA EXAMINATION, (C-14) JUNE—2019

## DCE-FOURTH SEMESTER EXAMINATION

ENGINEERING MATHEMATICS-III

## Time : 3 hours ]

## PART—A

Instructions: (1) Answer all questions.
(2) Each question carries three marks.

1. Solve $\left(D^{2}-5 D+6\right) y=0$.
2. Solve $\left(D^{3}+3 D^{2}-D+3\right) y=0$.
3. Find the particular integral of $\left(D^{2}+2 D+1\right) y=e^{3 x}$.
4. Find $L\left\{t^{2}+2 t+\cos 2 t\right\}$.
5. Find $L\left\{e^{2 t} \cdot \sin h 4 t\right\}$.
6. Find $L^{-1}\left\{\frac{2 s+3}{s^{2}+9}\right\}$.
7. Find $L^{-1}\left\{\frac{1}{(s+2)^{2}+16}\right\}$.
8. Write the Euler's formulae for Fourier series of a function $f(x)$ in the interval $(-\pi, \pi)$.
9. Find the $a_{0}$ for $f(x)=e^{x}$ in $(0,2 \pi)$.
10. When four coins are tossed simultaneously, find the probability of getting two heads and two tails.

## PART-B

$10 \times 5=50$
Instructions : (1) Answer any five questions.
(2) Each question carries ten marks.
11. (a) Solve $\left(D^{2}-3 D+2\right) y=5 e^{3 x}$.
(b) Solve $\left(D^{2}+4\right) y=\sin 2 x$.
12. Solve $\left(D^{2}+D-2\right) y=5+\sin x+x$.
13. (a) Find $L\left\{e^{12 t} \cdot \sin 5 t \cdot \cos 7 t\right\}$.
(b) Find $L\left\{t \cdot e^{-t} \cdot \sin 4 t\right\}$.
14. (a) Find $L^{-1}\left\{\frac{s}{s^{2}+4 s+13}\right\}$.
(b) Find $L^{-1}\left\{\frac{1}{(s+1) \cdot(s+3)}\right\}$.
15. Expand the function $f(x)=x+x^{2}$ as a Fourier series in $(-\pi, \pi)$.
16. Obtain Fourier series for the function $f(x)=x^{2}$ in $(-l, l)$.
17. (a) If $A$ and $B$ are mutually independent events, such that $P(A)=4$ and $P(B)=\frac{3}{5}$ then find $P(A \cup B)$.
(b) A fair die is rolled twice. What is the probability that an odd number will follow an even number?
18. These are three boxes I, II and III. Box I contains 4 red, 5 blue and 6 white balls. Box II contains 3 red, 4 blue and 5 white balls. Box III contains 5 red, 10 blue and 5 white balls. One box is chosen and one ball is drawn from it. What is the probability that-
(a) Red ball is drawn
(b) Blue ball is drawn
(c) White ball is drawn

