## C-14-CHPC/EC/PET-102

## 4034

## BOARD DIPLOMA EXAMINATION, (C-14) <br> APRIL/MAY-2015 <br> DECE-FIRST YEAR EXAMINATION

ENGINEERING MATHEMATICS—I
Time : 3 hours ]

Instructions: (1) Answer all questions.
(2) Each question carries three marks.
(3) Answer should be brief and straight to the point and shall not exceed five simple sentences.

1. Resolve $\frac{1}{(x-5)(x-7)}$ into partial fractions.
2. If $A=\left[\begin{array}{ccc}2 & 0 & 1 \\ 2 & 1 & 3 \\ 1 & -1 & 0\end{array}\right]$, then find $A^{2}$.
3. If $A=\left[\begin{array}{ll}1 & 3 \\ 2 & 1\end{array}\right]$, then find $A^{2}-3 A+2 I$, where $I$ is a unit matrix of order 2.
4. If $A+B=45^{\circ}$, then show that

$$
(1+\tan A)(1+\tan B)=2
$$

5. Prove that $\cot A-\cot 2 A=\operatorname{cosec} 2 A$.
[ Contd...
6. Find the modulus of the complex number $\frac{3+4 i}{1+7 i}$.
7. Find the equation of the straight line passing through the point $(3,-4)$ and perpendicular to the line $3 x+5 y-21=0$.
8. Find the equation of the circle having $(a, 0)$ and $(0, b)$ as the extremities of the diameter.
9. Evaluate $\lim _{x \rightarrow 5}\left(\frac{x^{3}-125}{x-5}\right)$.
10. Find the derivative of $\log [\log (\log x)]$.

## PART-B

Instructions : (1) Answer any five questions.
(2) Each question carries ten marks.
(3) Answers should be comprehensive and the criterion for valuation is the content but not the length of the answer.
11. (a) Show that

$$
\left|\begin{array}{lll}
1 & a & a^{2} \\
1 & b & b^{2} \\
1 & c & c^{2}
\end{array}\right|=(a-b)(b-c)(c-a)
$$

(b) Solve the equations $x+2 y-z=-1, \quad 3 x-y-2 z=5$ and $x-y-3 z=0$ by Cramer's rule.
12. (a) If $A+B+C=180^{\circ}$, then show that $\cos 2 A+\cos 2 B+\cos 2 C=-1-4 \cos A \cos B \cos C$
(b) Show that

$$
\tan ^{-1}\left[\frac{2}{7}\right]+\tan ^{-1}\left[\frac{1}{4}\right]=\cot ^{-1}\left[\frac{26}{15}\right]
$$

13. (a) Solve the equation $\sqrt{3} \cos \theta+\sin \theta=\sqrt{2}$.
(b) If $a \cos A=b \cos B$, prove that $\triangle A B C$ is either isosceles or right angled.
14. (a) Find the equation of the parabola with focus $(5,0)$ and directrix $x+y+1=0$.
(b) Find the lengths of the major and minor axis, length of latus recum (LLR), eccentricity and foci of the ellipse

$$
\frac{x^{2}}{25}+\frac{y^{2}}{16}=1
$$

15. (a) Find the derivative of $\frac{a-b \cos x}{a+b \cos x}$ with respect to $x$.
(b) Find $\frac{d y}{d x}$, if $y=\tan ^{-1}\left[\sqrt{\frac{1-\cos x}{1+\cos x}}\right]$.
16. (a) Find $\frac{d y}{d x}$, if $x=a \cos ^{3} \theta, y=b \sin ^{3} \theta$.
(b) If $u=\log \left(x^{2}+y^{2}\right)$, then prove that $\frac{\partial^{2} u}{\partial y \partial x}=\frac{\partial^{2} u}{\partial x \partial y}$.
17. (a) Find the equations of tangent and normal to the curve $y^{2}=4 a x$ at the point $\left(a t^{2}, 2 a t\right)$.
(b) A circular metal plate expands by heat so that its radius is increasing at the rate 0.02 cm per second. At what rate its area is increasing when the radius is 20 cm ?
18. (a) A wire of length 40 cm is bent so as to form a rectangle. If its area is to be maximum, find dimensions of the rectangle.
(b) The circumference of a circle is measured as 28 cm with an error of 0.04 cm . Find the approximate percentage error in the area of the circle.
