## 4461

## BOARD DIPLOMA EXAMINATION, (C-14)

OCT/NOV-2018

## DEEE-FOURTH SEMESTER EXAMINATION

## ENGINEERING MATHEMATICS-III

## PART—A

Instruction: (1) Answer all questions. Each question carries three marks.
(2) Answers should be brief and straight to the point and shall not exceed five simple sentences.

1. Solve $\left(D^{2}+5 D-6\right) y=0$, where $D=\frac{d}{d x}$.
2. Solve $\left(D^{3}-2 D^{2}-D+2\right) y=0$, where $D=\frac{d}{d x}$.
3. Find the particular integral of $\left(D^{2}+9\right) y=\cos 3 x$.
4. Find

$$
L\left\{e^{2 t}+4 t^{3}+\cos 3 t\right\}
$$

5. Find

$$
L\left\{t^{3} \cdot e^{-3 t}\right\}
$$

6. Find

$$
L^{-1}\left\{\frac{s^{2}-3 s+4}{s^{3}}\right\}
$$

7. Find

$$
L^{-1}\left\{\frac{1}{(s+2)^{2}}\right\}
$$

8. Find the value of $a_{0}$ in $f(x)=x \cos x$ in the interval $[0,2 \pi]$.
9. Write down the formulae for Fourier coefficients and Fourier series expansion of a function $f(x)$ in the interval $(C, C+2 l)$
10. Find the probability of getting all heads when three coins are tossed once.

## PART—B

$10 \times 5=50$

Instruction: (1) Answer any five questions and each question carries ten marks.
(2) Answers should be comprehensive and the criteria for valuation is the content but not the length of the answers.
11. (a) Solve

$$
\left(D^{2}+D-6\right) y=e^{3 x}+e^{-3 x}
$$

(b) Solve

$$
\left(D^{2}+D-2\right) y=\sin x
$$

12. Solve

$$
\left(D^{2}+5 D+4\right) y=\left(x^{2}+7 x+9\right)+\cos 2 x
$$

13. (a) Find

$$
L\left\{\frac{\sin 4 t}{t}\right\}
$$

(b) Find

$$
\left\{\frac{2 s}{(s-1)(s+2)}\right\}
$$

14. Solve $y^{11}+y=t$ using Laplace transform method given that

$$
y(0)=1 \text { and } y^{1}(0)=-2
$$

15. Obtain the Fourier series of $f(x)=x^{2}$ in the interval $[0,2 \pi]$.
16. Expand $f(x)=x$ in $0<x<2$ by Fourier half range cosine series.
17. (a) If 4 English, 5 Drawing and 6 Mathematics books are arranged in a shelf at random in a row, then find the probability that the books of each kind come tog.
(b) $A, B, C$ are three newspapers published from a city, $20 \%$ of people read $A$. $16 \% \operatorname{read} B, 14 \%$ read $C, 8 \%$ read both $A$ and $B, 5 \%$ read both $B$ and $C, 4 \%$ read both A and C and $2 \%$ read all three newspapers. Find the percentage of population who read at least 1 newspaper.
18. (a) A bag contains 6 red, 7 black and 8 blue balls. If two balls are drawn simultaneously what is the probability that one is read and the other is black.
(b) If $A$ and $B$ are any 2 events with $P(A)=\frac{1}{2}, P(B)=\frac{1}{3}$ and $P(A \cup B)=\frac{7}{12}$. Find $P\left(\frac{A}{B}\right)$ and $P\left(\frac{B}{A}\right)$.
