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BOARD DIPLOMA EXAMINATION, (C-20) OCTOBER/NOVEMBER—2023 DCE-THIRD SEMESTER (COMMON) EXAMINATION

ENGINEERING MATHEMATICS—II

Time: 3 Hours [Total Marks: 80

PART—A

 $3 \times 10 = 30$

Instructions: (1) Answer **all** questions.

(2) Each question carries three marks.

1. Evaluate
$$\int (x^7 - \frac{3}{x} + \sin x) dx$$

2. Evaluate
$$\int \frac{\cos(\log x)}{x} dx$$

- **3.** Evaluate $\int \sin 8x \cos 3x \, dx$
- **4.** Evaluate $\int x^3 e^{2x} dx$
- **5.** Evaluate $\int_0^1 \frac{1}{1+x^2} dx$
- **6.** Find the mean value of $y = x^3 + x$ between x = 0 and x = 1.
- **7.** Find the area bounded by the curve $y = x^2$, X-axis between x = 1 and x = 2.
- **8.** Find the differential equation of the family of curves $y = A \cos x + B \sin x$, where A and B are arbitrary constants.

9. Solve
$$\frac{dy}{dx} + \sqrt{\frac{1 - y^2}{1 - x^2}} = 0$$

10. Solve
$$x^4 dx + y^4 dy = 0$$

PART—B

 $8 \times 5 = 40$

Instructions: (1) Answer any five questions.

(2) Each question carries eight marks.

11. (a) Evaluate $\int \frac{1}{4+5\cos x} dx$

(OR)

(b) Evaluate
$$\int \frac{1}{x^2 + 4x + 13} dx$$

12. (a) Evaluate $\int \sin^4 x \cos^3 x \, dx$

(OR)

(b) Evaluate
$$\int x \tan^{-1} x \, dx$$

13. (a) Evaluate
$$\int_0^{\frac{\pi}{2}} \frac{\sqrt{\sin x}}{\sqrt{\sin x} + \sqrt{\cos x}} dx$$
 (OR)

(b) Show that
$$\int_{-1}^{1} \log \left(\frac{3-x}{3+x} \right) dx = 0$$

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14. (a) Find the R.M.S value of $\sqrt{27-4x^2}$ from x=0 to x=3.

(OR)

- (b) Find the area enclosed between the curve $y = x^2$ and the line 2x y + 3 = 0.
- **15.** (a) Evaluate $\int_0^1 \frac{1}{1+x} dx$ using trapezoidal rule by taking n = 4

(OR)

(b) Find the volume generated by the revolution of the ellipse $9x^2 + 25y^2 = 225$ about X-axis.

PART—C

 $10 \times 1 = 10$

Instructions: (1) Answer the following question.

- (2) The question carries ten marks.
- **16.** Solve $(x^2 + y^2) dx = 2xy dy$.

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