C20-C-CM-401

7424

BOARD DIPLOMA EXAMINATION, (C-20) JUNE/JULY—2022

DACE – FOURTH SEMESTER EXAMINATION

ENGINEERING MATHEMATICS-III

Time: 3 hours [Total Marks: 80

PART—A 3×10=30

Instructions: (1) Answer all questions.

(2) Each question carries three marks.

1. Solve
$$(D^2 + 1)y = 0$$

2. Solve
$$(D^2 + 4D + 6)y = 0$$

- 3. Find the particular integral of differential equation $(D^2 4D + 8)y = e^{-x}.$
- 4. Find the particular integral of differential equation $(D^2 16)y = \sin 2x$.
 - 5. Find $L\{2e^{-7t} + 5t^3 + 2\sinh 2t\}$.
 - 6. Find $L\left\{e^{-t}\cos 2t\right\}$.
 - 7. Find $L^{-1}\left\{\frac{1}{s^2+4s+20}\right\}$.

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- 8. Write down the Fourier series expansion of a function f(x) in the interval (-1,1). Give the corresponding formulae for finding the coefficients.
- 9. Obtain the value of " b_n " in Fourier series expansion of $f(x) = \cos x$ in the interval $-\pi < x < \pi$.
- 10. Obtain the value of " a_0 " in the half range cosine series expansion of f(x) = 3x + 1 in the interval 0 < x < 2.

PART—B 8×5=40

Instructions: (1) Answer either (a) or (b) from each questions from part-B.

(2) Each question carries eight marks.

11. (a) Solve
$$(D^4 - D^3 - 9D^2 - 11D - 4)Y = 0$$

(b) Solve
$$(D^2 - 3D + 2)y = (e^x + 1)^2$$

12. (a) Solve
$$(D^2 + 5D - 6)y = \sin 4x \sin x$$

(OR)

(b) Solve
$$(D^2 + 4)y = x^2 + 3$$

13. (a) Find
$$L(f(t))$$
 if $f(t) = \begin{cases} 1, & 0 < t < 2 \\ 2, & t > 2 \end{cases}$
(OR)

(b) Evaluate $L\{t(\sin t + \cos t)\}$

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- 14. (a) Evaluate $L \left\{ \frac{\cos at \cos bt}{t} \right\}$
 - (OR) $(b) \quad \text{Evaluate } L^{-1} \left\{ \frac{s+1}{s^2 + 6s 7} \right\}$
- 15. *(a)* Find $L^{-1}\left\{\frac{s}{(s-1)(s-2)}\right\}$

(b) Find $L^{-1} \left\{ \frac{s}{\left(s^2+1\right)^2} \right\}$ by using convolution theorem.

PART—C 10×1=10

Instructions: (1) Answer the following question.

(2) The question carries ten marks.

16. Find the Fourier series for $f(x) = x^2$ in the interval $(0, 2\pi)$.

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