

Subject Code: H2103/R13

M. Tech –II Semester Regular/ Supply Examinations, October, 2015
FINITE ELEMENT METHOD

(Common to TE, MD, MED, CAD/CAM, AMS and AM&MSD)

Time: 3 Hours

Max Marks: 60

Answer any FIVE questions
 All questions carry EQUAL marks

1. Construct the weak form and the quadratic potential if it exists for the following problem

Longitudinal deformation of a bar with an end spring:

$$-\frac{d}{dx} \left(a \frac{du}{dx} \right) = q \quad \text{for } 0 < x < L$$

$$u(0) = 0, \quad \left(a \frac{du}{dx} + ku \right) \Big|_{x=L} = P$$

where a and q are functions of x , and k and P are constants.

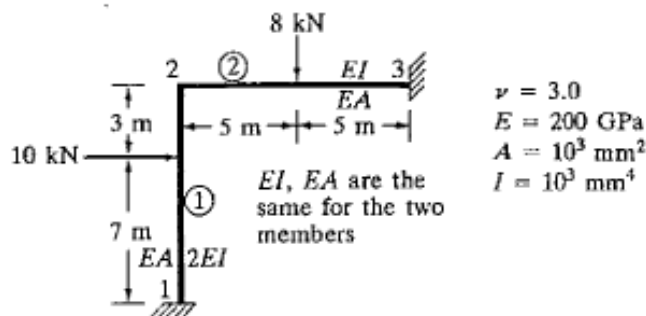
2. Compute the coefficient matrix and the right-hand side of the N-parameter Rayleigh-Ritz

approximation of the equation $-\frac{d}{dx} \left[(1+x) \frac{du}{dx} \right] = 0$ for $0 < x < 1$
 $u(0) = 0, \quad u(1) = 1$

Use algebraic polynomials for the approximation functions, Specialize your result for N=2 and compute the Ritz coefficients

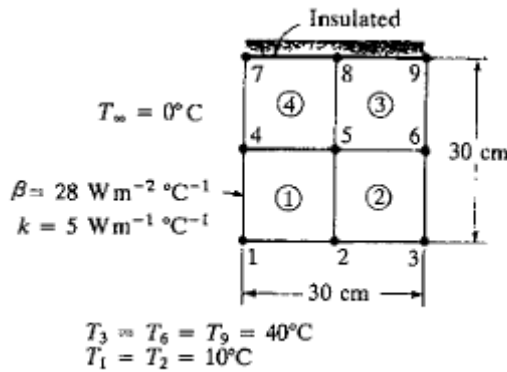
3. For the problem shown

- (a) Give the transformed element matrices
- (b) Assembled element matrices
- (c) The condensed matrix equations for the unknown generalized displacements and forces.



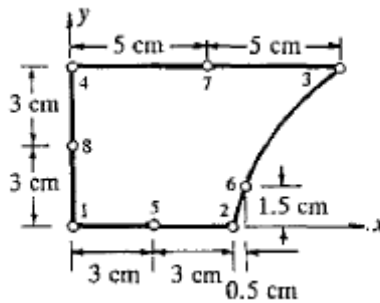
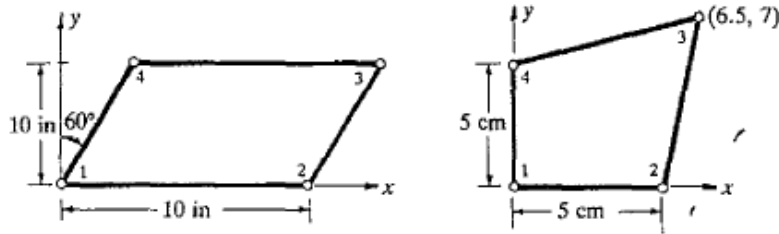
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4. Write the finite element equations for the unknown temperatures of the following problem



5. Determine the smallest natural frequency of a beam with damped ends, and a constant cross-sectional area A , moment of inertia I , and length L . Use the symmetry and two Euler – Bernoulli beam elements in the half-beam

6. Determine the jacobian and the transformation equations for the following



7. The transverse displacement of a triangular bending element (w) is expressed as a complete third degree polynomial in x and y . The nodal degrees of freedom are the displacements and the partial derivatives. Determine whether the convergence requirements are satisfied by this model.

- 8. a) Discuss in detail serendipity and Lagrange interpolation functions
- b) Explain how boundary conditions are handled in FEM
- c) Derive the characteristic matrix for two dimensional fin

