

I B. Tech II Semester Supplementary Examinations, April/May - 2019
MATHEMATICS-II
 (Com. to All Branches)

Time: 3 hours

Max. Marks: 75

Answer any **FIVE** Questions
 All Questions carry **Equal** Marks

1. a) Find the $L \left\{ \int_0^t e^{-2t} \sqrt{t} dt \right\}$ (8M)
 b) Find $L\{f'(t)\}$ of the function $f(t) = \begin{cases} 3, & 0 \leq t < 2 \\ 0, & t \geq 2 \end{cases}$ (7M)
2. a) Find $L^{-1} \left\{ \frac{s+2}{s^2(s+3)} \right\}$ (8M)
 b) Find $L^{-1} \left\{ \log \left(\frac{s+1}{s-1} \right) \right\}$ (7M)
3. a) Find the Fourier series of $f(x) = \cos x$ in $(-\pi, \pi)$. (8M)
 b) Find the Half range cosine series of $f(x) = x^2$ in $[0, 2]$. (7M)
4. a) Find the Fourier cosine transform of $\frac{1}{1+x^2}$ (8M)
 b) Find the Fourier transform of $f(x) = \begin{cases} x & \text{if } 0 < x < 1 \\ 1-x & \text{if } 1 < x < 2 \end{cases}$ (7M)
5. a) Prove that $\Gamma(n)\Gamma(1-n) = \frac{\pi}{\sin n\pi}$ (8M)
 b) Evaluate $\int_0^1 x^4 \left(\log \frac{1}{x} \right)^4 dx$ (7M)
6. a) Form the PDE from $z = f(2x+3y)+g(3x-y)$ by eliminating arbitrary functions. (8M)
 b) Solve the PDE $p \operatorname{cosec} x + q \operatorname{cosec} y = \operatorname{cosec} z$. (7M)
7. A bar of length l with insulated sides is initially 0°C temperature throughout the end $x = 0$ is kept at 0°C for all time and heat is suddenly applied such that $\frac{\partial u}{\partial x} = 10$ at $x = l$ for all time. Find the temperature function $u(x, t)$. (15M)
8. a) Solve the difference equations $u_{n+1} + \frac{1}{4}u_n = \left(\frac{1}{4}\right)^n, n \geq 0, u(0) = 0, u_1 = 1$ using Z-transform method. (8M)
 b) Find $Z[\sin(3n + 5)]$ (7M)