

**MATHEMATICS-II**  
(Common to All Branches)

**Time: 3 hours**

**Max. Marks: 75**

**Answer any FIVE Questions**  
**All Questions carry equal marks**

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1. (a) Evaluate  $L(t^2 u(t-2))$   
 (b) Find The Laplace transform of  $\sinh t/t$  [8+7]
  
2. (a) Find inverse Laplace transform of  $\frac{1+e^{-\pi s}}{s^2+1}$   
 (b) Solve the equation  $y^{111} + 2y^{11} - y^1 - 2y = 0$ ,  $y(0) = y^1(0) = y^{11}(0) = 6$  using Laplace transform method. [7+8]
  
3. (a) Find the Half range cosine series of  $f(x) = e^x$  in  $[0, \pi]$   
 (b) Expand  $f(x) = x \sin x$   $(-1, 1)$  as a Fourier series [7+8]
  
4. (a) Find the Fourier sine transform of  $f(x) = \frac{1}{x(x^2+a^2)}$   
 (b) Find the Fourier transforms  $f(x) = e^{-a|x|}$  ( $a > 0$ ) and hence deduces that  $\frac{\pi}{2a} e^{-a|x|} = \int_0^\infty \frac{\cos sx}{s^2+a^2} ds$  [7+8]
  
5. (a) Solve the PDE  $\left(\frac{y-z}{yz}\right)p + \left(\frac{z-x}{xz}\right)q = \left(\frac{x-y}{xy}\right)r$   
 (b) Solve the PDE  $z^2(x^2 p^2 + q^2) = 1$  [7+8]
  
6. (a) Solve by method of separation of variables  $2x \frac{\partial z}{\partial x} - 3y \frac{\partial z}{\partial y} = 0$   
 (b) Solve the one dimensional wave equation. [5+10]
  
7. (a) Find Z transform of (i)  $\cosh at$  (ii)  $\sinh at$   
 (b) Find  $Z^{-1} \left[ \frac{z^3 - 20z}{(z-2)^3(z-4)} \right]$  [8+7]
  
8. (a) Prove that  $\Gamma(n)\Gamma(1-n) = \frac{\pi}{\sin n\pi}$   
 (b) Evaluate  $\int_0^\infty \sqrt{x} e^{-x^2} dx$  [7+8]