

Subject Code: R13202/R13

Set No - 1

I B.Tech II Semester Supplementary Examinations Dec./Jan. – 2015/2016

MATHEMATICS-III

(Common to All Branches)

Time: 3 hours

Max. Marks: 70

Question Paper Consists of **Part-A** and **Part-B**
Answering the question in **Part-A** is Compulsory,
Three Questions should be answered from **Part-B**

PART-A

1. (a) Find the Rank of the matrix $\begin{bmatrix} 0 & 1 & 2 \\ 1 & 4 & 2 \\ 2 & 6 & 5 \end{bmatrix}$ using Echelon form
- (b) Prove that the matrix A and A^T have same Eigen values
- (c) Find the volume of loop of the curve $2ay^2 = x(x - a)^2$ revolves about x-axis
- (d) Evaluate $\int_0^1 x^5 (1 - x^3)^{10} dx$
- (e) Prove that $\text{div}(r \times a) = 0$ where a is a constant vector
- (f) Evaluate $\int f \cdot dr$ where $f = (2y + 3)i + xzj + (yz - x)k$ along the straight line joining (0,0,0) and (2,1,1)

[3+3+4+4+4+4]

PART-B

2. (a) Test for consistency and solve $5x + 3y + 7z = 4, 3x + 26y + 2z = 9, 7x + 2y + 10z = 5$.
- (b) Solve the equations
 $xy + z - w = 2, 7x + y + 3z + w = 12, 8x - y + z - 3w = 5, 10x + 5y + 3z + 2w = 20$. by Gauss-Jordan method

[8+8]

3. (a) Verify Cayley Hamilton theorem for $A = \begin{bmatrix} 1 & 0 & 3 \\ 2 & 1 & -1 \\ 1 & -1 & 1 \end{bmatrix}$, hence compute A^4 and A^{-1}

- (b) Reduce the quadratic form $3x^2 + 5y^2 + 3z^2 - 2yz + 2zx - 2xy$ in to canonical form by orthogonal reduction hence find rank, index and signature .

[8+8]

4. (a) Trace the curve $x = a \cos^3 \theta, y = b \sin^3 \theta$

- (b) Evaluate the $\int_0^a \int_{x/a}^{\sqrt{x/a}} (x^2 + y^2) dx dy$ by change of order of integration

[8+8]

5. (a) Prove that $\nabla \cdot (\bar{f} \times \bar{g}) = \bar{g} \cdot (\nabla \times \bar{f}) - \bar{f} \cdot (\nabla \times \bar{g})$

(b) Find the angle between the surfaces $x^2 + y^2 - z^2 = 12$ & $x^2 + y^2 - z = 5$ at $(2, 2, 1)$

[8+8]

6. (a) Evaluate $\iint_s x^3 dydz + x^2 ydzdx + x^2 zdx dy$ over the surface bounded by the planes

$z = 0, z = b$ and the cylinder $x^2 + y^2 = a^2$.

(b) Evaluate $\iiint_v 45x^2 y dx dy dz$ and v is the region bounded by $x = y = z = 0$ and $4x + 2y + z = 8$

[8+8]

7. (a) Evaluate $\int_0^{\infty} 3^{-4x^2} dx$

(b) Prove that $\Gamma(n)\Gamma(1-n) = \pi / \sin n\pi$

[8+8]
