

I B. Tech I Semester Supplementary Examinations, March – 2022**MATHEMATICS-II (MM)****(Com to AE, AME, Bio Tech, Chem. E, CE, EEE, ME, Metal E, Min E, PCE, PE)**

Time: 3 hours

Max. Marks: 70

Note: 1. Question Paper consists of two parts (**Part-A** and **Part-B**)2. Answer **ALL** the question in **Part-A**3. Answer any **FOUR** Questions from **Part-B**

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**PART -A**

1. a) Find the interval of existence of equation  $x^4 = x + 10$  (2M)
- b) Write a formula for the half range cosine series of  $f(x)$  in  $[0,2]$  (2M)
- c) Write a formula for the Fourier cosine transform (2M)
- d) Find  $\Delta(\sin 2x)$  if  $h = 1$  (2M)
- e) Find  $y(1.2)$  given that by Euler's method  $\frac{dy}{dx} = 2x + y$ ,  $y(1) = 1$  (2M)
- f) What are the advantages of RK method (2M)
- g) Write D Alembert's solution of wave equation (2M)

**PART -B**

2. a) Find the Real root of  $e^x \sin x = 1$  using False position method (7M)
- b) Find the Real root of  $x^3 - x - 4 = 0$  using Iteration method (7M)
3. a) Find the Lagrange's polynomial for the following data (7M)

|   |   |   |   |
|---|---|---|---|
| x | 0 | 1 | 2 |
| y | 1 | 2 | 3 |

- b) Find  $y(1.5)$  from the following data (7M)

|   |    |    |    |    |
|---|----|----|----|----|
| x | 1  | 2  | 3  | 4  |
| y | 20 | 35 | 45 | 60 |

- 4 a) Evaluate  $\int_0^{\pi} \sin x dx$  using Simpson's 1/3<sup>rd</sup> rule (7M)
- b) Using RK method of second order find  $y(0.1)$ ,  $y(0.2)$  given that  $\frac{dy}{dx} = 2y + 3e^x$ ,  $y(0) = 0$  (7M)

5. a) Find the Fourier series of  $f(x) = \begin{cases} x + \pi & -\pi < x < 0 \\ x - \pi & 0 < x < \pi \end{cases}$  (7M)

b) Find the Half range sine series of  $f(x) = \begin{cases} 1 - x & 0 < x < 1 \\ x - 2 & 1 < x < 2 \end{cases}$  (7M)

6. a) Solve the PDE  $\frac{\partial^2 u}{\partial x^2} = \frac{\partial u}{\partial y} + 2u$  by the method of variable separable method (7M)

b) Derive the four conditions to Solve the wave equation  $\frac{\partial^2 y}{\partial x^2} = c^2 \frac{\partial^2 y}{\partial t^2}$  (7M)

7. a) Do the Fourier sine and cosine transform exist for  $e^x$  (7M)

b) Find the Fourier integral representation of  $f(x) = \begin{cases} 1 - x^2 & \text{if } |x| \leq 1 \\ 0 & \text{if } |x| > 1 \end{cases}$  (7M)