

I B. Tech II Semester Supplementary Examinations, Nov/Dec - 2017**MATHEMATICS-II (MM)**

(Com. to CE,EEE,ME,AE,AME,Bio-Tech,Chem E,Metal E,Min E,PCE,PE)

Time: 3 hours

Max. Marks: 70

Note: 1. Question Paper consists of two parts (**Part-A** and **Part-B**)2. Answer **ALL** the question in **Part-A**3. Answer any **FOUR** Questions from **Part-B****PART -A**

1. a) Write the geometrical interpretation of Newton-Raphson method. (2M)
- b) Prove that $\delta = 2\sin \frac{hD}{2}$. (2M)
- c) Write Newton Back word interpolation formula. (2M)
- d) Write the Taylor's series to solve the D.E $\frac{dy}{dx} = f(x, y), y(x_0) = y_0$ (2M)
- e) Find the value of b_n in the half range sine series of $f(x) = \sin x$ in $[0, \pi]$. (2M)
- f) Write the Dirichlet conditions for Fourier Transforms. (2M)
- g) Write two dimensional Laplace equation. (2M)

PART -B

2. a) Find the Real root of $x^4 - x - 9 = 0$ using False position method. (7M)
- b) Find the Real root of $x = 2\sin x$ using Iteration method. (7M)
3. a) Find the Missing term in the following data. (7M)

x	1	2	3	4	5
y	7	--	13	21	37

- b) Find $f(32)$ using Gauss Backward interpolation formula from the following table. (7M)

x	25	30	35	40
y	0.2707	0.3027	0.3386	0.3794

4. a) Evaluate $\int_0^1 \sqrt{1+x^4} dx$ by taking $h = 0.125$ by (i) Simpson's $1/3^{\text{rd}}$ rule (ii) Simpson's $3/8^{\text{th}}$ rule. (7M)

- b) Evaluate $y(0.1)$ using RK method of fourth order for $\frac{dy}{dx} = y - \frac{2x}{y}$, $y(0) = 1$ (7M)

5. a) Expand $f(x) = \begin{cases} x, & -\frac{\pi}{2} < x < \frac{\pi}{2} \\ \pi - x, & \frac{\pi}{2} < x < \frac{3\pi}{2} \end{cases}$ as half range cosine series. (7M)

b) Expand $f(x) = \begin{cases} 4 - x, & 3 < x < 4 \\ x - 4, & 4 < x < 5 \end{cases}$ Fourier series. (7M)

6. a) Express the $f(x) = \begin{cases} 1 & \text{if } 0 < x < \pi \\ 0 & \text{if } x > \pi \end{cases}$ as a Fourier sine integral. (7M)

Hence Evaluate $\int_0^{\infty} \frac{(1 - \cos \lambda \pi) \sin \lambda x}{\lambda} d\lambda$

b) Find the Fourier transform of $f(x)$ defined by $f(x) = \begin{cases} 1 & \text{if } |x| < a \\ 0 & \text{if } |x| > a \end{cases}$ (7M)

(or)

And hence evaluate $\int_0^{\infty} \frac{\sin p}{p} dp \left[\int_0^{\infty} \frac{\sin x}{x} dx \right] \& \int_{-\infty}^{\infty} \frac{\sin ap \cos px}{p} dp$

7. a) Solve the PDE $\frac{\partial^2 u}{\partial x^2} = 16 \frac{\partial u}{\partial y}$ using method of variation of parameters. (7M)

b) A rod of length 100 cm length has its ends A and B kept at 0°C and 100°C until steady state conditions prevail. The temperatures at the ends are changed to 20°C and 60°C respectively. Find the temperature in the rod. (7M)