

**I B. Tech II Semester Supplementary Examinations, Nov/Dec - 2018****MATHEMATICS-II (MM)**

(Com. to CE,EEE,ME,AE,AME,Bio-Tech,Chem E,Metal E,Min E,PCE,PE)

Time: 3 hours

Max. Marks: 70

Note: 1. Question Paper consists of two parts (**Part-A** and **Part-B**)2. Answering question in **Part-A** is Compulsory3. Answer any **FOUR** Questions from **Part-B**

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**PART -A**

1. a) Write the two approximations of  $x \log_{10} x = 1.2$  by Newton Raphson method. (2M)
- b) Define Average operator. (2M)
- c) Write the demerits of Picard's method. (2M)
- d) Write Formula for Simpson's  $1/3^{\text{rd}}$  rule. (2M)
- e) Write Dirichlet conditions on Fourier transform. (2M)
- f) Write the half range sine series in  $(0, L)$ . (2M)
- g) Write the linear solution of wave (one dimensional) equations. (2M)

**PART -B**

2. a) Find the Real root of the equation  $x^3 + 2x^2 + 10x - 20 = 0$  using Bisection method. (7M)
- b) Find the Real root of the equation  $xe^x = \cos x$  using false position method. (7M)
3. a) Find  $f(0.5)$  using the data  $(0,5)$ ,  $(1,1)$ ,  $(2,8)$ ,  $(3,15)$ ,  $(4,25)$ ,  $(5,30)$ . (7M)
- b) Find the polynomial satisfied by  $(1, 2)$ ,  $(3,3)$ ,  $(4,5)$ ,  $(6,9)$ . (7M)
4. a) Find  $y(0.2)$ ,  $y(0.4)$  given that  $y' = \frac{1}{2}xy$ ,  $y(0) = 1$  by modified Euler's method. (7M)
- b) Evaluate  $\int_1^2 \frac{dx}{x}$  using (i) Simpson's  $1/3^{\text{rd}}$  rule with  $h = 0.5$  (ii) Trapezoidal rule with  $h = 0.25$ . (7M)

5. a) Find the half range cosine series  $f(x) = \begin{cases} -x, & 0 < x < \frac{\pi}{2} \\ x, & \frac{\pi}{2} < x < \pi \end{cases}$  (7M)

- b) Find the Fourier series for  $f(x) = \begin{cases} x, & 1 < x < 2 \\ 0, & 2 < x < 3 \end{cases}$  (7M)

6. a) Find the Fourier sine and cosine transform exist for  $e^x$  (7M)

b) Find the Fourier transform of  $f(x) = \begin{cases} 1, & |x| < a \\ 0, & |x| > a \end{cases}$  (7M)

$$\text{Deduce that } \int_0^{\infty} \frac{\sin t}{t} dt = \frac{\pi}{2} \text{ and } \int_0^{\infty} \frac{\sin^2 t}{t^2} dt = \frac{\pi}{2}$$

7. a) Solve the PDE  $\frac{\partial u}{\partial x} - 2 \frac{\partial u}{\partial y} = u$  and  $u(x, 0) = 3e^{-5x} + 2e^{-3x}$  (7M)

b) A Rod of length 10 cm has its ends A and B kept at  $50^\circ \text{C}$  and  $100^\circ \text{C}$  until steady state conditions prevail. The temperature at A is then suddenly raised to  $90^\circ \text{C}$  and that at B is lowered to  $60^\circ \text{C}$  and the end temperatures are there after maintained. Find the temperature at a distance  $x$  from one end at a time. (7M)

