

## I B. Tech II Semester Supplementary Examinations, January/February - 2023

## MATHEMATICS-II

(Com. to EEE,ECE,CSE,EIE,IT)

Time: 3 hours

Max. Marks: 75

*Answer any FIVE Questions ONE Question from Each Unit  
All Questions Carry Equal Marks*

## UNIT - I

1. a) Define the rank of the matrix and find the rank of the matrix using Echelon form [8M]

$$\begin{bmatrix} 1 & 1 & 3 & 5 \\ 2 & 2 & 1 & 3 \\ 4 & 4 & 7 & 3 \\ 2 & 4 & 3 & 1 \end{bmatrix}$$

- b) Solve the equations  $25x + 2y + 2z = 69, 2x + 10y + z = 63, x + y + z = 43$  [7M]  
by Gauss-Elimination method.

(OR)

2. a) Solve the equations  $x - 2y + z - w = 0, x + y - 2z + 3w = 0, 4x + y - 5z + 8w = 0, 5x - 7y + 2z - w = 0$ . [8M]

- b) Prove that the Eigen values of diagonal matrix are its diagonal elements. [7M]

## UNIT - II

3. a) Verify Cayley -Hamilton theorem for the matrix  $A = \begin{bmatrix} 2 & 1 & 1 \\ 0 & 1 & 0 \\ 1 & 1 & 2 \end{bmatrix}$  also find  $A^{-1}$  [8M]

- b) Find the nature, rank, index and signature of the quadratic form by reduce in to canonical form  $x^2 + 3y^2 + 3z^2 - 2yz$ . [7M]

(OR)

4. Reduce the quadratic form  $2x^2 + 4y^2 + 4z^2 + 2xy - 2xz + 6yz$  into a sum of squares by orthogonal transformation. [15M]

## UNIT - III

5. a) Find the real root of the equation  $x^3 - 5x - 7 = 0$  using Iteration method. [8M]

- b) Find the real root of the equation  $x \tan x + 1 = 0$  using bisection method. [7M]

(OR)

6. a) Find the real root of the equation  $x^3 - 8x + 4 = 0$  using Newton Raphson method [8M]

- b) Solve the following system of equations using Gauss-Jacobi method [7M]  
 $10x + y - 2z = 7, 3x + 10y - z = 8, 2x + y + 10z = 10$ .

## UNIT - IV

7. a) Find  $f(1.5)$  using Newton's Forward formula for the following table [8M]

X	1	2	3	4	5	6
Y	1	6	8	15	25	36

- b) Find  $\Delta^3[(1 - 2x)(1 - 3x^2)]$  [7M]

**(OR)**

8. a) Find
- $f(2.5)$
- using Newton's forward formula for the following table [8M]

X	1	2	3	4	5
Y	3	4	10	13	24

- b) Find the polynomial for the following data using Newton divided difference formula. [7M]

X	5	6	9	11
Y	12	13	14	16

**UNIT - V**

9. a) Find
- $y(0.1)$
- using RK method of second order If
- $\frac{dy}{dx} = \log(x + y)$
- ,
- $y(0) = 1$
- . [8M]

- b) By modified Euler's formula find
- $y(0.2)$
- given that
- $\frac{dy}{dx} = y - \frac{2x}{y}$
- ,
- $y(0) = 1$
- . [7M]

**(OR)**

- 10 a) Evaluate
- $\int_0^\pi \sin 2x \, dx$
- using Simpson's
- $1/3^{\text{rd}}$
- rule. [8M]

- b) By Picard's method find
- $y(0.1)$
- given that
- $\frac{dy}{dx} = 1 + xy$
- ,
- $y(0) = 1$
- . [7M]

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