

**I B. Tech II Semester Regular Examinations, December - 2020**  
**MATHEMATICS-II**  
 (Com. to EEE, ECE, CSE, EIE, IT)

Time: 3 hours

Max. Marks: 75

**Answer any five Questions one Question from Each Unit**  
**All Questions Carry Equal Marks**

1. a) Find the rank of  $\begin{bmatrix} 2 & 3 & -1 & -1 \\ 1 & -1 & -2 & -4 \\ 3 & 1 & 3 & -2 \\ 6 & 3 & 0 & -7 \end{bmatrix}$  after reducing it to echelon form. (8M)

b) Prove that If  $\lambda$  is an eigen value of a non singular matrix A, then  $\frac{|A|}{\lambda}$  is an eigen value of the matrix adj A. (7M)

Or

2. a) Find the eigenvalues and eigen vectors of  $\begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$ . (8M)

b) Show that the system  $x + 2y - 5z = -9$ ,  $3x - y + 2z = 5$ ,  $2x + 3y - z = 3$ ,  $4x - 5y + z = -3$  is consistent and solve it. (7M)

3. a) Verify Cayley-Hamilton theorem for  $A = \begin{bmatrix} 10 & 1 & 1 \\ 1 & 10 & -1 \\ 1 & -2 & 10 \end{bmatrix}$  and find  $A^{-1}$ . (8M)

b) Find a singular value decomposition for the matrix  $\begin{bmatrix} 1 & 1 \\ 1 & 0 \\ 0 & 1 \end{bmatrix}$ . (7M)

Or

4. Reduce the quadratic form  $2x^2 + 2y^2 + 2z^2 - 2xy + 2zx - 2yz$  to orthogonal transformation. Also find signature and rank of the quadratic form. (15M)

5. a) Find a real root of  $x \tan x + 1 = 0$  using iteration method. (6M)

b) Perform two iterations of the Newton-Raphson method to solve the system of equations  $x^2 + y^2 + xy = 7$  and  $x^3 + y^3 = 9$ . (9M)

Or

6. a) Using Gauss Seidel method to solve  $25x + 2y + 2z = 69$ ,  $2x + 10y + z = 63$ ,  $x + y + z = 43$ . (9M)

b) Find a real root of the equation  $x^3 - 4x - 9 = 0$  using false position method correct to three decimal places. (6M)

7. a) The population of a nation in the decennial census is given below. Estimate the population in the year 1925 using appropriate interpolation formula. (9M)

Year x	1891	1901	1911	1921	1931
Population y (thousands)	46	66	81	93	101

- b) Evaluate (i)  $\Delta^2 \sin(px + q)$  (ii)  $\Delta^n e^{ax+b}$  (6M)

Or

8. a) Find Interpolating polynomial by Lagrange's method and hence find  $f(2)$  for the following data. (6M)

x	0	1	3	4
f(x)	-12	0	6	12

- b) Determine  $f(x)$  as a polynomial in  $x$  for the following data using Newton's divided difference formula. (9M)

x	1	3	6	9	11
f(x)	12	33	41	55	133

9. a) Evaluate  $\int_0^1 \frac{x}{x^3 + 5} dx$  using Trapezoidal rule. (7M)

- b) Solve  $y' = x - y^2, y(0) = 1$  using Taylor's series method and compute  $y(0.1), y(0.2)$ . (8M)

Or

10. a) Using Euler's method, solve for  $y(2)$ , from  $\frac{dy}{dx} = 3x^2 + 1, y(1) = 2$ , taking  $h = 0.5$  (7M)

- b) Find  $y(0.1)$  using Runge-Kutta fourth order formula given that  $y' = x + x^2 y; y(0) = 1$ . (8M)

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1. a) Find the rank of the matrix by reducing it to normal form  $\begin{bmatrix} 1 & 2 & 2 & 4 \\ 2 & 3 & 4 & 6 \\ 3 & 5 & 6 & 10 \\ -1 & 1 & -2 & -2 \end{bmatrix}$ . (8M)
- b) Prove that the sum of the eigenvalues of a square matrix is equal to its trace and product of the eigenvalues is equal to its determinant. (7M)

Or

2. a) Find the eigenvalues and the corresponding eigen vectors of  $\begin{bmatrix} 1 & 2 & -2 \\ 1 & 1 & 1 \\ 1 & 3 & -1 \end{bmatrix}$ . (8M)
- b) Solve the system of equations  $x + 2y + 3z = 1$ ,  $2x + 3y + 8z = 2$ ,  $x + y + z = 3$  using Gauss elimination method. (7M)

3. a) Verify Cayley-Hamilton theorem for  $A = \begin{bmatrix} 3 & 1 & 2 \\ 2 & -3 & 1 \\ 1 & 2 & 1 \end{bmatrix}$  and find  $A^{-1}$ . (8M)

- b) Find a singular value decomposition for the matrix  $\begin{bmatrix} 1 & 0 \\ 1 & 0 \\ 0 & 1 \end{bmatrix}$ . (7M)

Or

4. Reduce the quadratic form  $2x^2 + 2y^2 + 2z^2 - 2xy + 2zx - 2yz$  to orthogonal transformation. Also find signature and rank of the quadratic form. (15M)
5. a) Find a real root of  $x^2 - \log_e x = 1.2$  using Regula falsi method. (6M)
- b) Perform two iterations of the Newton-Raphson method to solve the system of equations  $x^2 + 3y^2 = 4$  and  $x^2 + 3x + y = 5$ . (9M)

Or

6. a) Solve the system of equations  $20x + 2y + 6z = 28$ ,  $x + 20y + 9z = -23$  and  $2x - 7y - 20z = -57$  using Gauss Seidel method. (9M)
- b) Find a real root of  $x \tan x + 1 = 0$  using iteration method. (6M)

7. a) Find  $f(2.4)$  from the following data using appropriate interpolation method. (9M)

x	1.0	1.5	2.0	2.5
f(x)	3	3.375	5.0	12.072

- b) Prove that (i)  $\Delta\nabla = \Delta - \nabla$  (ii)  $\frac{\Delta}{\nabla} - \frac{\nabla}{\Delta} = \Delta + \nabla$ . (6M)

Or

8. a) Find Interpolating polynomial by Lagrange's method and hence find  $f(2)$  for the following data. (7M)

x	0	1	3	4
f(x)	-12	0	6	12

- b) Determine  $f(x)$  as a polynomial in  $x$  for the following data using Newton's divided difference formula. (8M)

x	0	2	3	5	8
f(x)	1	3	5	9	11

9. a) Evaluate  $\int_0^1 \frac{x}{x^3+5} dx$  using Simpson's 1/3<sup>rd</sup> rule. (8M)
- b) Solve  $y' = xy + 1$  and  $y(0) = 1$  using Taylor's series method compute  $y(0.01)$ ,  $y(0.02)$ . (7M)

Or

10. a) Using Euler's method, solve  $y' = y^2 + x$ ,  $y(0) = 1$ , compute  $y(0.1)$ ,  $y(0.2)$  (8M)

- b) Using Runge-Kutta fourth order formula, Find  $y(0.2)$  for the equation (7M)

$$y' = \frac{y-x}{y+x} \quad y(0) = 1.$$

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1. a) Reduce the matrix to normal form and hence find the rank of the matrix. (8M)

$$\begin{bmatrix} 1 & 2 & 3 & -2 \\ 2 & -2 & 1 & 3 \\ 3 & 0 & 4 & 1 \end{bmatrix}.$$

- b) If  $\lambda$  is an eigenvalue of A, then prove that the eigenvalue of  $B = a_0A^2 + a_1A + a_2I$  is  $a_0\lambda^2 + a_1\lambda + a_2$ . (7M)

Or

2. a) Find the eigenvalues and the corresponding eigen vectors of  $\begin{bmatrix} 6 & 3 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$  (9M)

- b) Solve  $x - y + 2z = 4$ ,  $3x + y + 4z = 6$ ,  $x + y + z = 1$  using Gauss elimination method. (6M)

3. a) Verify Cayley-Hamilton theorem for  $A = \begin{bmatrix} 3 & 1 & 2 \\ 2 & -3 & 1 \\ 1 & 2 & 1 \end{bmatrix}$  and find  $A^{-1}$ . (8M)

- b) Find a singular value decomposition for the matrix  $\begin{bmatrix} 1 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ . (7M)

Or

4. Reduce the quadratic form  $4x^2 + 3y^2 + z^2 - 8xy - 6yz + 4zx$  to orthogonal transformation. Also find signature and rank of the quadratic form. (15M)

5. a) Find a real root of  $x \sin x + \cos x = 0$  using Regula falsi method. (6M)

- b) Solve the system of nonlinear equations  $x^2 + y = 11$  and  $x + y^2 = 7$  By Newton-Raphson method. (9M)

Or

6. a) Solve the system of equations  $10x + 2y + z = 9$ ,  $2x + 20y - 2z = -44$  and  $-2x + 3y + 10z = 22$  using Gauss Seidel method. (9M)

- b) Solve  $x = 1 + \tan^{-1} x$  by iteration method. (6M)

7. a) Consider following data. (9M)

X	0.2	0.5	0.8	1.1	1.4
g(x)	9.9833	4.9696	3.2836	2.4339	1.9177

Calculate approximately  $g(0.15)$  using Newton's Forward Interpolation.

- b) Prove that  $\Delta \tan^{-1}\left(\frac{n-1}{n}\right) = \tan^{-1}\left(\frac{1}{2n^2}\right)$  (6M)

Or

8. a) Evaluate  $f(10)$  given that the value of  $f(x)$  at  $x = 2, 6, 12$  are  $16, 19, 33$  respectively. (8M)

- b) Determine  $f(x)$  as a polynomial in  $x$  for the following data using Newton's divided formula. (7M)

x	3	7	9	10
f(x)	160	120	72	63

9. a) Evaluate  $\int_0^2 e^{-x^2} dx$  using Simpson's 1/3 rd rule taking  $h = 0.25$ . (7M)

- b) Solve  $y' = 5x - y$  and  $y(1) = 1$  by Picard's method compute  $y(1.1)$ . (8M)

Or

10. a) Using Euler's method, solve for  $y(2)$ , from  $y' = 3x^2 + 1; y(1) = 2$ , taking step size  $h=0.5$ . (6M)

- b) Using Runge-Kutta fourth order formula, Find  $y(0.2)$  for the equation (9M)

$$y' = \frac{y-x}{y+x} \quad y(0) = 1.$$

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1. a) Find the rank of the matrix by reducing it to normal form  $\begin{bmatrix} 0 & 1 & -3 & -1 \\ 1 & 0 & 1 & 1 \\ 3 & 1 & 0 & 2 \\ 1 & 1 & -2 & 0 \end{bmatrix}$ . (8M)
- b) If  $\lambda$  is an eigen value of a matrix  $A$ , then  $\lambda^n$  is an eigen value of the matrix  $A^n$ . (7M)

Or

2. a) Find the eigen values and eigen vectors of  $\begin{bmatrix} -3 & -7 & -5 \\ 2 & 4 & 3 \\ 1 & 2 & 2 \end{bmatrix}$ . (9M)
- b) Find the value of 'b' such that the system of homogeneous equations  $2x+y+2z=0$ ,  $x+y+3z=0$ ,  $4x+3y+bz=0$  has (i) trivial solution (ii) Non-trivial solution. Find the non trivial solution. (6M)

3. a) Verify Cayley-Hamilton theorem for the matrix  $A = \begin{bmatrix} 1 & 2 & -1 \\ 2 & 1 & -2 \\ 2 & -2 & 1 \end{bmatrix}$  and find  $A^{-1}$ . (8M)
- b) Find a singular value decomposition for the matrix  $\begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \end{bmatrix}$ . (7M)

Or

4. Reduce the quadratic form  $4x^2 + 3y^2 + z^2 - 8xy - 6yz + 4zx$  to orthogonal transformation. Also find signature and rank of the quadratic form. (15M)
5. a) Find a real root of  $x \tan x + 1 = 0$  using iteration method. (6M)
- b) Solve the system of nonlinear equations  $xy = x + 9$  and  $y^2 = x^2 + 7$ . By Newton-Raphson method. (9M)

Or

6. a) Solve the system of equations  $10x+2y+z=9$ ,  $2x+20y-2z=-44$  and  $-2x+3y+10z=22$  using Jacobi method. (7M)
- b) Find a real root of the equation  $x^3 - 4x - 9 = 0$  using false position method correct to three decimal places. (8M)

7. a) The population of a nation in the decadal census was given below. Estimate the population in the year 1975 using appropriate interpolation formula. (9M)

Year x	1961	1971	1981	1991	2001
Population y (thousands)	66	76	81	93	105

- b) Evaluate (i)  $\Delta \left[ \frac{f(x)}{g(x)} \right]$  (ii) Prove that  $\nabla E = E \Delta = \Delta$ . (6M)

Or

8. a) Using Lagrange's Interpolation formula find the value of  $y(10)$  from the following table. (8M)

x	5	6	9	11
y(x)	12	13	14	16

- b) Determine  $f(x)$  as a polynomial in  $x$  for the following data using Newton's divided formula. (7M)

x	-4	-1	0	2	5
f(x)	1245	33	5	9	1335

9. a) Evaluate  $\int_0^1 \sqrt{1+x^4} dx$  using Simpson's 3/8 rule. (8M)
- b) Solve  $y' + y = e^x$  and  $y(0) = 0$  using Picard's method compute  $y(0.1)$  (7M)

Or

10. a) Using Euler's method, find  $y(0.2)$  and  $y(0.4)$ , given  $y' = x + y$ ,  $y(0) = 1$ . (6M)
- b) Find  $y(0.1)$ ,  $y(0.2)$  using Runge-Kutta fourth order formula given that  $y' = x + x^2 y$ ;  $y(0) = 1$ . (9M)